## Sixth Math Scope and Sequence

|  | Quarter 1 | Quarter 2 | Quarter 3 | Quarter 4 |
| :---: | :---: | :---: | :---: | :---: |
| Domain | Number System | Ratios and Proportions | Expressions and Equations | Geometry and Statistics |
| RATIOS AND PROPORTIONAL RELATIONSHIPS <br> 6.RP <br> Understand ratio concepts and use ratio reasoning to solve problems. <br> THE <br> NUMBER SYSTEM <br> 6NS <br> 1) Apply and extend previous <br> understandings of multiplication and division to divide fractions by fractions. 2-4) Compute fluently with multidigit numbers and find common factors and multiples. <br> 5-8) Apply and extend previous understandings of numbers to the system of rational numbers. <br> EXPRESSIONS AND EQUATIONS <br> 6.EE <br> 1-4) Apply and extend previous | 6.NS.1. Interpret and compute quotients of fractions, and solve word problems involving division of fractions by fractions, e.g., by using visual fraction models and equations to represent the problem. For example, create a story context for $(2 / 3) \div(3 / 4)$ and use a visual fraction model to show the quotient; use the relationship between multiplication and division to explain that $(2 / 3) \div(3 / 4)=8 / 9$ because $3 / 4$ of $8 / 9$ is $2 / 3$. (In general, $(a / b) \div(c / d)=a d / b c$.) How much chocolate will each person get if 3 people share $1 / 2$ lb of chocolate equally? How many 3/4-cup servings are in $2 / 3$ of a cup of yogurt? How wide is a rectangular strip of land with length $3 / 4 \mathrm{mi}$ and area 1/2 square mi? <br> 6.NS.2. Fluently divide multidigit numbers using a standard algorithm. <br> 6.NS.3. Fluently add, subtract, multiply, and divide multi-digit decimals using the standard algorithm for each operation. <br> 6.NS.4. Find the greatest common factor of two whole numbers less than or equal to 100 and the least common multiple of two whole numbers less than or equal to 12 . Use the | 6.RP.1. Understand the concept of a ratio and use ratio language to describe a ratio relationship between two quantities. For example, "The ratio of wings to beaks in the bird house at the zoo was 2:1, because for every 2 wings there was 1 beak." "For every vote candidate A received, candidate C received nearly three votes." <br> 6.RP.2. Understand the concept of a unit rate a/b associated with a ratio $a: b$ with $b \neq 0$, and use rate language in the context of a ratio relationship. For example, "This recipe has a ratio of 3 cups of flour to 4 cups of sugar, so there is $3 / 4$ cup of flour for each cup of sugar." "We paid \$75 for 15 hamburgers, which is a rate of $\$ 5$ per hamburger."(non complex fractions) <br> 6.RP.3a. Make tables of equivalent ratios relating quantities with whole number measurements, find missing values in the tables, and plot the pairs of values on the coordinate plane. Use tables to compare ratios. <br> 6.RP.3b. Solve unit rate problems including those involving unit pricing and constant speed. For example, if | 6.EE.1. Write and evaluate numerical expressions involving whole-number exponents. <br> 6.EE.2a. Write expressions that record operations with numbers and with letters standing for numbers. For example, express the calculation "Subtract y from 5 " as $5-y$. <br> 6.EE.2b. Identify parts of an expression using mathematical terms (sum, term, product, factor, quotient, coefficient); view one or more parts of an expression as a single entity. For example, describe the expression $2(8+7)$ as a product of two factors; view $(8+7)$ as both a single entity and a sum of two terms. <br> 6. EE.2c. Evaluate expressions at specific values of their variables. Include expressions that arise from formulas used in real-world problems. Perform arithmetic operations, including those involving whole number exponents, using the algebraic order of operations when there are no parentheses to specify a particular order. For example, use the formulas $V=s^{3}$ and $A=$ $6 s^{2}$ to find the volume and surface area of a cube with sides of length $s=1 / 2$. | 6.G. 1 Through composition into rectangles or decomposition into triangles, find the area of right triangles, other triangles, special quadrilaterals, and polygons; apply these techniques in the context of solving real-world and mathematical problems. <br> 6.G.3. Draw polygons in the coordinate plane given coordinates for the vertices; use coordinates to find the length of a side joining points with the same first coordinate or the same second coordinate. Apply these techniques in the context of solving real-world and mathematical problems. <br> 6.G.4. Represent threedimensional figures using nets made up of rectangles and triangles, and use the nets to find the surface area of these figures. Apply these techniques in the context of solving real-world and mathematical problems. <br> 6.G. 2 Find the volume of a right rectangular prism with fractional edge lengths by packing it with unit cubes of the appropriate unit fraction edge lengths, and show that the volume is the same as would be found by multiplying the edge lengths of the prism. Apply the formulas $V=\ell \cdot w \cdot h$ and $V=B$ - $h$ to find volumes of right rectangular prisms with fractional |

## understandings of

arithmetic to
algebraic
expressions.
5-8) Reason about and solve onevariable equations and inequalities.
9) Represent and analyze quantitative relationships between dependent and independent variables.

## GEOMETRY

6.G
1-4) Solve real-world
and mathematical
problems involving
area, surface area, and volume.

## STATISTICS

AND PROBABILITY
6.SP
1-3) Develop
understanding of statistical problem solving.
4-5) Summarize and describe distributions.
distributive property to express a sum of two whole numbers 1100 with a common factor as a multiple of a sum of two whole numbers with no common factor. For example, express 36 +8 as $4(9+2)$.
6.NS.5. Understand that positive and negative numbers are used together to describe quantities having opposite directions or values (e.g., temperature above/below zero, elevation above/below sea level, credits/debits, positive/negative electric charge); use positive and negative numbers to represent quantities in realworld contexts, explaining the meaning of 0 in each situation.
6.NS.6a. Recognize opposite signs of numbers as indicating locations on opposite sides of 0 on the number line; recognize that the opposite of the opposite of a number is the number itself, e.g., $-(-3)=3$, and that 0 is its own opposite.
6.NS.6c. Find and position integers and other rational numbers on a horizontal or vertical number line diagram; find and position pairs of integers and other rational numbers on a coordinate plane.
6.NS.7a. Interpret statements of inequality as statements about the relative position of two numbers on a number line diagram. For example, interpret $-3>-7$ as a statement that -3
it took 7 hours to mow 4 lawns, then at that rate, how many lawns could be mowed in 35 hours? At what rate were lawns being mowed?
6.RP.3c. Find a percent of a quantity as a rate per 100 (e.g., $30 \%$ of a quantity means 30/100 times the quantity); solve problems involving finding the whole, given a part and the percent.
6.EE.3. Apply the properties of operations to generate equivalent expressions. For example, apply the distributive property to the expression $3(2+$ x) to produce the equivalent expression $6+3 x$; apply the distributive property to the expression $24 x+18 y$ to produce the equivalent expression $6(4 x+$ 3y); apply properties of operations to $y+y+y$ to produce the equivalent expression $3 y$.
6.EE.4. Identify when two expressions are equivalent (i.e., when the two expressions name the same number regardless of which value is substituted into them). For example, the expressions $y+y+y$ and $3 y$ are equivalent because they name the same number regardless of which number y stands for.
6.EE.5. Understand solving an equation or inequality as a process of answering a question: which values from a specified set, if any, make the equation or inequality true? Use substitution to determine whether a given number in a specified set makes an equation or inequality true.
6.EE.6. Use variables to represent numbers and write expressions when solving a realworld or mathematical problem; understand that a variable can represent an unknown number, or, depending on the purpose at hand, any number in a specified set.
edge lengths in the context of solving real-world and mathematical problems.
6.SP. 1 Develop statistical reasoning by using the GAISE model:
1a. Formulate Questions: Recognize and formulate a statistical question as one that anticipates variability and can be answered with quantitative data. For example, "How old am I?" is not a statistical question, but "How old are the students in my school?" is a statistical question because of the variability in students' ages. (GAISE Model, step 1)
1b. Collect Data: Design and use a plan to collect appropriate data to answer a statistical question. (GAISE Model, step 2)
6.SP.2. Understand that a set of data collected to answer a statistical question has a distribution which can be described by its center, spread, and overall shape.
6.SP.3. Recognize that a measure of center for a numerical data set summarizes all of its values with a single number, while a measure of variation describes how its values vary with a single number.
6.SP. 1 Develop statistical reasoning by using the GAISE model:
1c. Analyze Data: Select appropriate graphical methods and numerical measures to analyze data by displaying variability within a group, comparing individual to

## is located to the right of -7 on a number line oriented from left to right.

6.NS.7b. Write, interpret, and explain statements of order for rational numbers in real-world contexts. For example, write $-3^{\circ} \mathrm{C}>-7^{\circ} \mathrm{C}$ to express the fact that $-3^{\circ} \mathrm{C}$ is warmer than $-7^{\circ} \mathrm{C}$.
6.NS.7c. Understand the absolute value of a rationa number as its distance from 0 on the number line; interpret absolute value as magnitude for a positive or negative quantity in a real-world situation. For example, for an account balance of -30 dollars, write $|-30|=30$ to describe the size of the debt in dollars.
6.NS.7d. Distinguish comparisons of absolute value from statements about order. For example, recognize that an account balance less than -30 dollars represents a debt greater than 30 dollars.
6. NS.6b. Understand signs of numbers in ordered pairs as indicating locations in quadrants of the coordinate plane; recognize that when two ordered pairs differ only by signs, the locations of the points are related by reflections across one or both axes.
6.NS.8. Solve real-world and mathematical problems by graphing points in all four quadrants of the coordinate
6.EE.7. Solve real-world and mathematical problems by writing and solving equations of the form $x+p=q$ and $p x=q$ for cases in which $p, q$ and $x$ are all nonnegative rational numbers.
6.EE.8. Write an inequality of the form $x>c$ or $x<c$ to represent a constraint or condition in a realworld or mathematical problem. Recognize that inequalities of the form $x>c$ or $x<c$ have infinitely many solutions; represent solutions of such inequalities on number line diagrams.
6.EE.9. Use variables to represent two quantities in a real world problem that change in relationship to one another; write an equation to express one quantity, thought of as the dependent variable, in terms of the other quantity, thought of as the independent variable. Analyze the relationship between the dependent and independent variables using graphs and tables, and relate these to the equation. For example, in a problem involving motion at constant speed, list and graph ordered pairs of distances and times, and write the equation $d=$ $65 t$ to represent the relationship between distance and time.
individual, and comparing individual to group. (GAISE Model, step 3)
1d. Interpret Results: Draw logical conclusions from the data based on the original question. (GAISE Model, step 4)
6.SP. 4 Display numerical data in plots on a number line, including dot plotsG (line plots), histograms, and box plotsG. (GAISE Model, step 3)
6.SP.5a. Reporting the number of observations.
6.SP.5b. Describing the nature of the attribute under investigation, including how it was measured and its units of measurement.
6.SP. 5 c . Find the quantitative measures of center (median and/or mean) for a numerical data set and recognize that this value summarizes the data set with a single number. Interpret mean as an equal or fair share. Find measures of variability (range and interquartile range) as well as informally describe the shape and the presence of clusters, gaps, peaks, and outliers in a distribution.
6.SP.5d. Choose the measures of center and variability, based on the shape of the data distribution and the context in which the data were gathered.

|  | plane. Include use of coordinates and absolute value to find distances between points with the same first coordinate or the same second coordinate. |  |  |  |
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| Resources | Reveal Math Modules 3, 4, 5, 6, 7 ODE Model Curriculum GAISE model framework | Reveal Math <br> Modules 1, 2, 7, 10 <br> ODE Model Curriculum <br> GAISE model framework | Reveal Math Modules 5, 6, 7, 8, 9, 10 ODE Model Curriculum GAISE model framework | Reveal Math <br> Modules 8, 9, 10 <br> ODE Model Curriculum <br> GAISE model framework |

## CRITICAL AREAS

Critical Area 1: Connecting ratio and rate to whole number multiplication and division and using concepts of ratio and rate to solve problems Students use reasoning about multiplication and division to solve ratio and rate problems about quantities. By viewing equivalent ratios and rates as deriving from, and extending, pairs of rows (or columns) in the multiplication table, and by analyzing simple drawings that indicate the relative size of quantities, students connect their understanding of multiplication and division with ratios and rates. Thus students expand the scope of problems for which they can use multiplication and division to solve problems, and they connect ratios and fractions. Students solve a wide variety of problems involving ratios and rates.
Critical Area 2: Completing understanding of division of fractions and extending the notion of number to the system of rational numbers, which includes negative numbers Students use the meaning of fractions, the meanings of multiplication and division, and the relationship between multiplication and division to understand and explain why the procedures for dividing fractions make sense. Students use these operations to solve problems. Students extend their previous understandings of number and the ordering of numbers to the full system of rational numbers, which includes negative rational numbers, and in particular negative integers. They reason about the order and absolute value of rational numbers and about the location of points in all four quadrants of the coordinate plane.
Critical Area 3: Writing, interpreting, and using expressions and equations Students understand the use of variables in mathematical expressions. They write expressions and equations that correspond to given situations, evaluate expressions, and use expressions and formulas to solve problems. Students understand that expressions in different forms can be equivalent, and they use the properties of operations to rewrite expressions in equivalent forms. Students know that the solutions of an equation are the values of the variables that make the equation true. Students use properties of operations and the idea of maintaining the equality of both sides of an equation to solve simple one-step equations. Students construct and analyze tables, such as tables of quantities that are in equivalent ratios, and they use equations (such as $3 x=y$ ) to describe relationships between quantities.
Critical Area 4: Developing understanding of statistical problem solving Building on and reinforcing their understanding of number, students begin to develop their ability to think statistically. The GAISE model is used as a statistical problem solving framework. Students recognize that a data distribution may not have a definite center and that different ways to measure center yield different values. The median measures center in the sense that it is roughly the middle value. The mean measures center in the sense that it is the value that each data point would take on if the total of the data values were redistributed equally, and also in the sense that it is a balance point. Students recognize that a measure of variability (range and interquartile range) can also be useful for summarizing data because two very different sets of data can have the same mean and median yet be distinguished by their variability. Students learn to describe and summarize numerical data sets, identifying clusters, gaps, peaks, and outliers in a distribution, considering the context in which the data were collected.
Critical Area 5: Solving problems involving area, surface area, and volume Students in Grade 6 also build on their work with area in elementary school by reasoning about relationships among shapes to determine area, surface area, and volume. They find areas of right triangles, other triangles, and special quadrilaterals by decomposing these shapes, rearranging or removing pieces, and relating the shapes to rectangles. Using these methods, students discuss, develop, and justify formulas for areas of triangles and parallelograms. Students find areas of polygons and surface areas of prisms and pyramids by decomposing them into pieces whose area they can determine. They reason about right rectangular prisms with fractional side lengths to extend formulas for the volume of a right rectangular prism to fractional side lengths. They prepare for work on scale drawings and constructions in Grade 7 by drawing polygons in the coordinate plane.

